

$$\int_0^{\infty} t^x e^{-t} \frac{dt}{t} = \frac{1}{x} \prod_{k=1}^{\infty} \frac{(1 + \frac{1}{k})^x}{(1 + \frac{x}{k})}$$