Math 502

Written Assignment No. 2

due Wednesday, March 7, 2007

Directions: Use *Maple* for assistance in responding to the following problems. Please typeset your solutions. Explain what you have done. *Maple* session details are not necessary unless you think it important to include them. Accuracy is important.

Although you may refer to books and notes, you may **not** seek help from others on this written assignment.

Answer the following questions:

1. What is the length of the repeating pattern in the decimal expansion of

$$\frac{1}{1+2^{100}}$$
 ?

(Don't even think about trying to compute the expansion.)

2. If $P = a + bx + cx^2 + dx^3 + ex^4 + fx^5$ is a polynomial, find polynomials q_0, q_1, q_2, \ldots of degree at most 1 such that

$$P = \sum_{j \ge 0} q_j (x^2 + 1)^j .$$

- 3. Factor the polynomial $x^{31} 1$ as
 - (a) a rational polynomial.
 - (b) a polynomial mod 2.
 - (c) a polynomial mod 3.
 - (d) a polynomial mod 5.
- 4. Find the partial fraction expansion of

$$\frac{1}{r^{31}-1}$$

regarded as a "rational function" with coefficients mod 2.

5. The sequence of integers

is the sequence of 17-th powers mod 97 of numbers obtained from a sequence of ASCII codes by left-shifting each code 30 units so the sequence occupies the interval [2, 96] instead of the normal printable ASCII interval [32, 126]. What text string led to the original sequence?